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## Mechanical Analysis and Performance Optimization for the Lunar Rover's Vane-Telescopic Walking Wheel



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### ABSTRACT

It is well-known that optimizing the wheel system of lunar rovers is essential. However, this is a difficult task due to the complex terrain of the moon and limited resources onboard lunar rovers. In this study, an experimental prototype was set up to analyze the existing mechanical design of a lunar rover and improve its performance. First, a new vane-telescopic walking wheel was proposed for the lunar rover with a positive and negative quadrangle suspension, considering the complex terrain of the moon. Next, the performance was optimized under the limitations of preserving the slope passage and minimizing power consumption. This was achieved via analysis of the wheel force during movement. Finally, the effectiveness of the proposed method was demonstrated by several simulation experiments. The newly designed wheel can protrude on demand and reduce energy consumption; it can be used as a reference for lunar rover development engineering in China.

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### 1. Introduction

Exploring the moon has become a globally important task. One of the most important tasks in moon exploration is lunar landing, such as those achieved by Chang'e 3 (China) and Apollo 13 (USA). In the future, manned lunar landings will be carried out (China: 2025 [1–3]; USA: restart Apollo [4]). Here, the key technique lies in the trafficability characteristic of the lunar rover. That is, the newly designed lunar rover should be able to walk in the complex and harsh environment of the lunar surface. For example, the surface temperature of the moon can reach 150 °C in the daytime and drop as low as –180 °C at night, which makes the wheel technology used on earth difficult to use on the moon.

For this purpose, the wheel should have the following features:  
① The lunar rover should be designed with high traction perfor-

mance and carrying capacity [5–9]; and ② the rover wheel should be able to traverse obstacles [10]. There is an irregular distribution of rocks, craters, and slopes of different sizes and shapes on the surface of the moon [11–16]. The particle size and softness of lunar soil vary greatly [17].

In this regard, many kinds of wheel structure have been designed. Three have successfully landed on the moon: the elastic wheel of the former Soviet Lunokhod [18], the spring-griddle net wheel used by the American Apollo lunar roving vehicle (LRV) [4], shown in Fig. 1, and the Chinese YuTu [1,19–21], shown in Fig. 2. Other research results on wheel structure include the cylinder-conical wheel developed by Harbin Institute of Technology and the grip-hook and intelligent variable-diameter wheels designed by Beihang University, which have strong adaptability with the surface of the moon (Fig. 3) [22–24].

Of these existing designed wheels, the spring-griddle net wheel is easily deformed when the load is extremely large, the cylinder-conical wheel and the intelligent variable-diameter wheel are liable to fracture upon impact, and the grip-hook wheel has a

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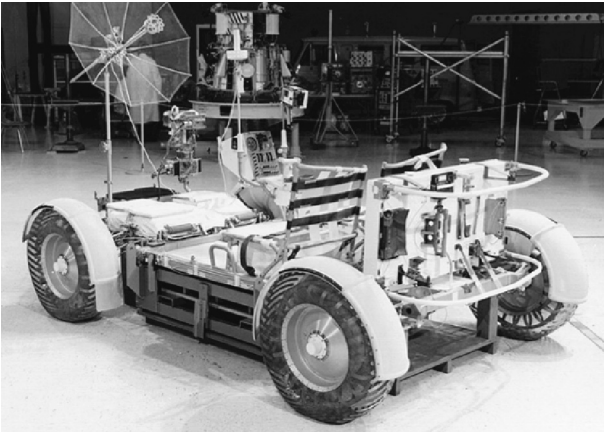


Fig. 1. The Apollo LRV.

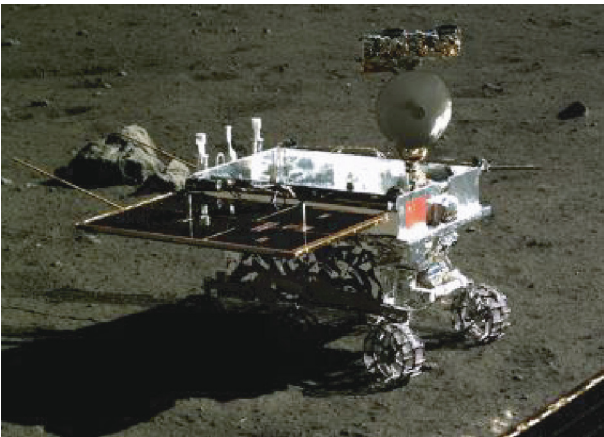


Fig. 2. YuTu and spring-griddle net wheel.

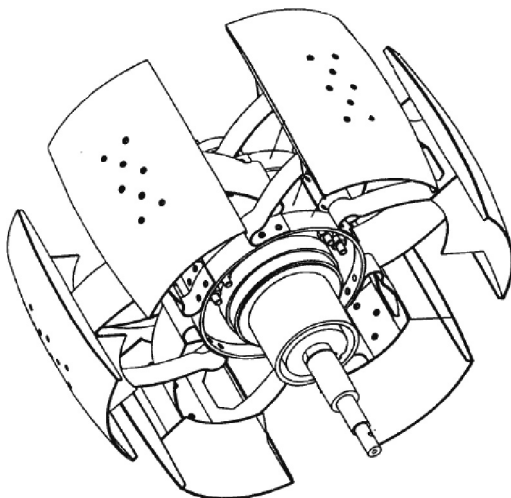


Fig. 3. The intelligent variable-diameter wheel.

complex structure and low reliability, so it is easily damaged. Furthermore, although these wheels have a strong ability to surmount obstacles, they are weak in power-consumption control and cannot meet the complex requirements of future lunar exploration projects [4]. Therefore, it is necessary to design new wheels with better balance.

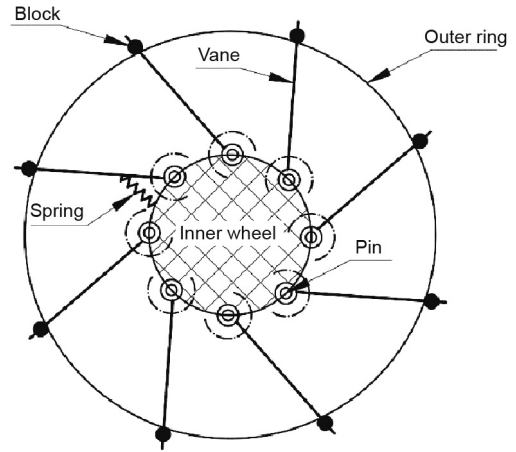


Fig. 4. Structure of vane-telescopic walking wheel.

To resolve these problems, a new wheel system is proposed. The system is based on the vane-telescopic walking wheel (Fig. 4), which was designed by the Intelligent Vehicle Group of Jilin University. This model was selected as the basis of our prototype, as it is suitable for lunar soft soil [25,26]. The most important merit of our new wheel system is that the wheel vane length can be adjusted automatically according to the road surface (i.e., softness and slope) and obstacles (i.e., size) [18].

For the vane-telescopic walking wheel, the longer the wheel vane is, the better the wheel passing performance is. Meanwhile, the greater the wheel rolling resistance is, the greater the energy consumption of the wheel is. Therefore, the ideal extension condition is for the wheel vane to protrude according to the terrain need, thus reducing the energy consumption [27].

In this study, a new wheel system is designed based on the following contributions, in order to pass through all kinds of road conditions on demand with the lowest energy consumption:

- (1) A new vane-telescopic walking wheel is proposed for the lunar rover with a positive and negative quadrangle suspension.
- (2) The parameters of the vane-telescopic walking wheel design are optimized.
- (3) The prototype is evaluated in a simulated lunar soil environment.
- (4) A new lunar rover prototype vehicle is designed and tested initially with the new wheel.

The remainder of this paper is organized as follows: Section 2 introduces the wheel force analysis for lunar rover wheels. Section 3 analyzes the parameter optimization of the vane-telescopic walking wheel design. Section 4 deals with the prototype evaluation in the simulated lunar soil environment. Section 5 concludes this paper and suggests several possible future works.

## 2. Force analysis for lunar rover wheels

Before optimizing the vane-telescopic walking wheel, the lunar rover wheel is analyzed based on the actual conditions on the lunar surface; the dimension of the designed wheels can then be determined based on the analysis results [28]. The paper is based on a lunar rover model with a positive and negative quadrangle suspension, which was proposed by the Intelligent Vehicle Group of Jilin University.

In Fig. 5,  $L_1 = 453.3$  mm,  $L_2 = 191.65$  mm,  $L_3 = 212.1$  mm,  $L_4 = 218.72$  mm,  $L_5 = 145.05$  mm,  $L_6 = 431.86$  mm,  $L_7 = 142.24$  mm,  $L_8 = 342.6$  mm,  $L_9 = 141.4$  mm,  $L_{10} = 354.2$  mm,  $L_{11} = 400.1$  mm,  $L_{12} = 135$  mm,  $\gamma_1 = 38.31^\circ$ ,  $\gamma_2 = 41.76^\circ$ ,  $\gamma_3 = 53.62^\circ$ ,  $\gamma_4 = 68.29^\circ$ ,  $\gamma_5 = 17.36^\circ$ ,  $\gamma_6 = 44.9^\circ$ ,  $\gamma_7 = 42.3^\circ$ ,

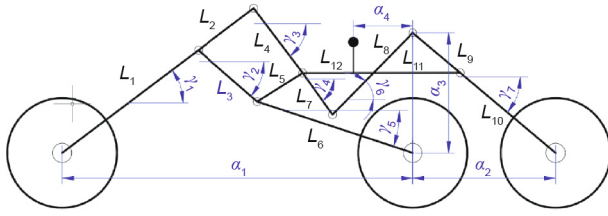


Fig. 5. Suspension rod angles and key suspension dimensions of the model.

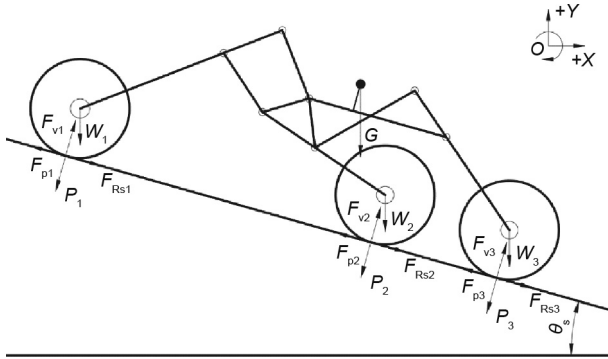


Fig. 6. The force of the mobile system on a road with a slope angel of  $\theta_s$ .

**Table 1**  
Slope resistance  $F_{Rs}$  and pressure  $P$  with varying slope  $\theta_s$ .

$\theta_s$ (°)	$F_{Rs1}/P_1$ (N)	$F_{Rs2}/P_2$ (N)	$F_{Rs3}/P_3$ (N)
0	0/30.6	0/36.9	0/30.6
5	2.4/27.8	3.2/36.3	2.9/33.6
10	4.4/24.9	6.2/35.1	6.5/36.6
15	5.9/21.9	8.9/33.1	10.6/39.7
20	6.9/18.9	11.0/30.3	15.7/43.0
25	7.5/16.1	16.8/36.1	21.8/46.7
30	7.9/13.7	11.5/20.0	29.6/51.3

$a_1 = 938.3$  mm,  $a_2 = 359.5$  mm,  $a_3 = 307.8$  mm, and  $a_4 = 179.1$  mm. Here,  $L_i$  is the length of suspension; whose horizontal angle is represented by  $\gamma_i$ ; while  $a_i$  means the length between two points. According to the design requirements of the mobile system, the wheel radius  $R$  is 150 mm, the single wheel mass is 3.5 kg, and the vehicle mass is 120 kg. Under the lunar gravity field, the weight of front ( $W_1$ ), middle ( $W_2$ ), and rear wheels ( $W_3$ ),  $W_1 = W_2 = W_3 = 5.7$  N, and gravity on one side of the load platform  $G = 80.85$  N.

The key road condition for a lunar rover is slope. In many of the road conditions that a lunar rover must pass, the slope is the most intuitive and effective factor to reflect the wheel force condition. When a lunar rover is climbing, the wheel force condition is the most serious parameter, and the traction performance requirement for the wheel is the highest priority [29]. In this paper, the wheel force analysis is carried out with a slope angel of  $\theta_s$  degrees (Fig. 6).

The road's supporting force  $F_v$  and the wheel's pressure  $P$  are a pair of counterforces that have equal values and opposite directions. The friction force  $F_p$  and the slope resistance  $F_{Rs}$  are also a pair of counterforces. Therefore, the slope resistance and the pressure on the road of the lunar rover can be obtained, as shown in Table 1.

### 3. Optimizing parameters determination of the vane-telescopic walking wheel

The most difficult challenge is the complex lunar environment, which consists of irregular stones and craters, varying slopes, and

lunar soil with varying granularity and softness. Traditional wheels cannot fully deal with such an environment because their traction ability is insufficient to pull the lunar rover in soft lunar soil. To resolve this problem, a new type of wheel is designed that can automatically retract vanes according to the soil characteristics. First, the forces between the wheels and soil are analyzed below.

#### 3.1. Force analysis between the wheels and soil

The force of the wheel can be divided into soil thrust (ST) and soil resistance (SR) according to the effectiveness of the force. If the ST is greater than the SR, the wheel will move forward. Otherwise, the wheel will rotate or remain stationary [30–33]. Here, SR includes four kinds of resistances: soil compaction resistance (SCR), soil bulldozing resistance (SBR), soil slope resistance (SSR), and soil vane resistance (SVR) [34]. The details of ST and four kinds of SR are introduced below.

##### 3.1.1. Compaction resistance

During the wheel rolling process, the soil is extruded vertically downward. At the same time, the soil forces the wheel to prevent the vertical extrusion from forming the wheel compaction resistance. The compaction resistance  $F_{Rc}$  can be expressed as follows [35,36]:

$$F_{Rc} = b_1 \times \left( \frac{z_0^{n+1}}{n+1} \right) \times \left( \frac{k_c}{b_1} + k_\phi \right) \quad (1)$$

where  $z_0$  is the sinking depth of the wheel rim,

$z_0 = \left[ \frac{3 \times P}{(k_c + b_1 \times k_\phi) \times \sqrt{D} \times (3-n)} \right]^{\frac{2}{2n+1}}$ ,  $k_c$  is the cohesion modulus of the soil,  $k_\phi$  is the friction modulus of the soil,  $n$  is the soil deformation index,  $b_1$  is the width of the wheel rim,  $D$  is the diameter of the wheel rim, and  $P$  is the pressure of the wheel on the soil.

##### 3.1.2. Bulldozing resistance

Aside from vertical compaction, soil deformation is caused by the push forward of the wheels; this is the SBR bulldozing resistance, in which the soil in front of the wheels is wave shaped [37]. The bulldozing resistance  $F_{Rb}$  can be expressed as follows:

$$F_{Rb} = b_1 \times \left( 0.67 \times c \times z_0 \times K'_c + 0.5 \times z_0^2 \times \gamma_s \times K'_\gamma \right) \quad (2)$$

where  $K'_c = [N'_c - \tan(\phi')] \times \cos^2(\phi')$ ,  $K'_\gamma = [2 \times N'_\gamma / \tan(\phi') + 1] \times \cos^2(\phi')$ ,  $\phi' = \arctan[(2/3)\tan(\phi)]$ ,  $\gamma_s$  is the bulk density,  $c$  is the cohesion force, and  $\phi$  is the internal friction angle.  $N'_c$  and  $N'_\gamma$  are the Terzaghi bearing coefficients, which are related to  $\phi$ ; their values are provided in Table 2 [38–40].

##### 3.1.3. Slope resistance

When the lunar rover climbs up a slope, the gravity in the direction of the slope creates the slope resistance [41], which can be expressed as follows:

$$F_{Rs} = W_i \times \sin(\theta_s) \quad (3)$$

where  $W_i$  is the weight of the  $i$ th wheel and  $\theta_s$  is the slope angle.

**Table 2**  
Terzaghi bearing coefficients.

$\phi$ (°)	$N'_c$	$N'_\gamma$
31	18	4
33	20	5
35	23	7
37	27	10
39	32	14
41	40	20

3.1.4. Vane resistance

During the rolling process, the wheel vanes compress the soil vertically, and the soil prevents the vertical extrusion force from forming the vane compacting resistance, which is known as the vane resistance [42]. The vane resistance  $F_{RV}$  can be expressed as follows:

$$F_{RV} = \frac{b_2 \times b \times N^{n+1} \times \sin^n(180^\circ/N) \times (1-S)^{n-1}}{\pi^{n+1} \times D \times (n+1)} \times h_b^{n+1} \times \left(\frac{k_c}{b_2} + k_\phi\right) \quad (4)$$

where  $N$  is the number of vanes,  $b$  is the vane thickness,  $b_2$  is the vane width,  $S$  is the slip ratio of the wheel, and  $h_b$  is the inserting depth of the vane. According to the sampling analysis of the lunar soil [43], the soil deformation index  $n$  is usually equal to 1, so the slip ratio index of the wheel  $S$  is  $n - 1 = 0$ . Thus, the vane resistance is not affected by the wheel slip ratio.

3.1.5. Soil thrust of the vane

The maximum ST received by the wheel rim,  $F_w$ , can be expressed as follows:

$$F_w = c \times A + P \times \tan\phi \quad (5)$$

where  $A$  is the contact area between the wheel rim and the soil:  $A = 2 \times b_1 \times \sqrt{D \times z_0 - z_0^2}$ .

The maximum ST received by the wheel vane,  $F_s$ , can be represented as follows:

$$F_s = b_2 \times \left(\frac{1}{2} \times \gamma_s \times h_b^2 \times N_\phi + q \times h_b \times N_\phi + 2c \times h_b \times \sqrt{N_\phi}\right) \quad (6)$$

where  $q$  is the pressure stress of the wheel rim on the soil,  $q = P/A$ ,  $N_\phi$  is the flow value of the soil, and  $N_\phi = \tan^2(45^\circ + \phi/2)$ . According to Eqs. (1)–(6), the maximum traction force of the wheels,  $F_d$ , can be expressed by Eq. (7).

$$F_d = F_w + F_s - F_{RC} - F_{Rb} - F_{Rs} - F_{RV} \quad (7)$$

3.2. Optimizing parameters determination

Optimization of the vane spring, which is the most important feature for the performance of the lunar rover wheel, is our key work. In this study, the vane spring stiffness  $k$  and the spring initial torque  $T_0$  are calculated as the optimization variables so that the wheels can endure various road conditions while consuming the lowest amount of energy.

The optimizing parameters include the minimum of the inserting depth of the vane into soil when the wheels pass  $h_b$ , the wheel rolling resistance torque  $T_f$ , the supporting force  $F_v$ , and the wheel friction force  $F_p$ . Some of the parameters are used as optimization constraints, and the others are used as the input of the optimization function. When calculating the above parameters, the follow-

ing road conditions are analyzed: high, medium, and low soil passing ability; and a slope of  $0^\circ$ – $30^\circ$  [44].

By introducing the lunar soil parameters, the wheel parameters, and the wheel slope resistance  $F_{Rs}$  (Table 1), we can obtain the minimum inserting depth  $h_b$  of the vane under various passing abilities of the soil and different degrees of the slope. The wheel pressure  $P$  (Table 1) and  $h_b$  obtained above are then taken into the wheel resistance Eqs. (1), (2), and (4), and the wheel rolling resistance is obtained. The resistance is multiplied by the wheel radius  $R$ —that is, the wheel rolling resistance torque  $T_f$ . Table 3 shows the optimization parameters of the front wheel [45].

4. Optimization design and experiment with the new wheel

As shown in Fig. 7, vane 5 ( $i = 5$ ) is located at the bottom of the wheel, and mainly acts with the soil. Therefore, the extension of vane 5 is considered in the following analysis. The extended length of vane 5 can be expressed as  $L_{o5}(\theta_s = 0^\circ) = L_{oi}$  ( $i = 5$ ,  $\theta_s = 0^\circ$ ), where the calculation of function  $L_{o5}$  is detailed in the Appendix A. The objective function of the vane spring optimization is as follows:

(1) The requirement of high passing ability [46]:  $L_{o5}(\theta_s) \geq h_b(\theta_s)$ ,  $\theta_s = 0^\circ, 5^\circ, \dots, 30^\circ$ .

(2) The requirement of reducing resistance and energy consumption [47]:  $\sum [L_{o5}(\theta_s) - h_b(\theta_s)]$  must be the minimum.

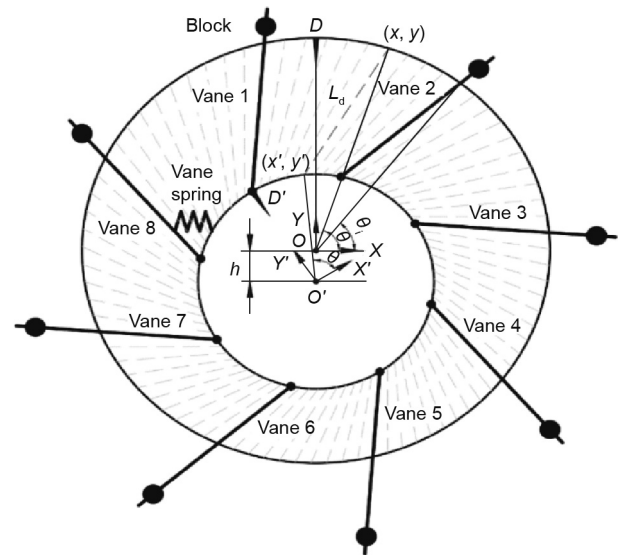


Fig. 7. The position of the vane spring.

Table 3 Optimization parameters of the front wheel.

Slope $\theta_s$ ( $^\circ$ )	Minimum inserting depth $h_b$ (mm)			Wheel rolling resistance torque $T_f$ (N·mm)			Supporting force $F_v$ (N)	Friction force $F_p$ (N)
	High soil passing ability	Middle soil passing ability	Low soil passing ability	High soil passing ability	Middle soil passing ability	Low soil passing ability		
0	0	0	0	631.6	739.8	848.9	30.6	0
5	0	0	0	55.7	650.9	746.9	27.8	2.4
10	1.2	3.2	4.7	480.2	565.0	651.2	24.9	4.4
15	5.3	9.6	12.2	412.7	500.7	586.5	21.9	5.9
20	8.7	17.0	20.1	354.9	474.4	563.6	18.9	6.9
25	14.5	22.4	29.2	331.4	462.2	607.6	16.1	7.5
30	20.3	28.5	42.8	340.0	492.9	821.5	13.7	7.9

4.1. Optimizing the design of the vane spring

The optimization parameters obtained in Section 3.2, including  $T_f$ ,  $F_p$ ,  $F_v$ , and  $h_b$ , are introduced into the above objective function to obtain Eq. (8).

$$\begin{cases} L_{o5}(\theta_{si} T_{fi} F_{pi} F_{vi}) \geq h_{bi} \\ \sum_{i=1}^{21} \{L_{o5}(\theta_{si} T_{fi} F_{pi} F_{vi}) - h_{bi}\} = \text{minimum} \end{cases}, i = 1, 2, \dots, 21 \quad (8)$$

where  $i$  represents 21 kinds of road conditions, which are composed of various slopes ( $\theta_s = 0^\circ, 5^\circ, 10^\circ, 15^\circ, 20^\circ, 25^\circ$ , and  $30^\circ$ ) and soil passing abilities (high, medium, and low).

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20	0.6087	6.9	18.9																																																																																																									
20	0.6340	6.9	18.9																																																																																																									
25	0.4051	7.5	16.1																																																																																																									
25	0.5700	7.5	16.1																																																																																																									
25	0.6499	7.5	16.1																																																																																																									
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The spring stiffness  $k$  and initial torque value  $T_0$  of the front wheel vanes are then obtained. According to this calculation, they are  $k = 0.112 \text{ N}\cdot\text{m}\cdot\text{rad}^{-1}$  ( $1 \text{ rad} = 180^\circ/\pi$ ) and  $T_0 = -0.038 \text{ N}\cdot\text{m}$ . A type of spring can be selected for the front wheel that can ensure the wheel's passing performance in the complex moon environment. It can also reduce the energy consumption from the excessive overhang of vanes [48–50].

4.2. Analysis of the optimization effect

In the function  $L_{o5}$ , the rolling resistance torque  $T_f$  and the wheel friction  $F_p$  are always formed by  $T_f + R \times F_p$ .  $T_f + R \times F_p$  can be regarded as a variable, and is called the rolling friction force  $T_v$ . Thus, three variables in the original function  $L_{o5}$  can be expressed in the form of two variables,  $T_v$  and  $F_v$  [51]. To analyze the mechanical properties for the front wheel optimization,  $k = 0.112$  and  $T_0 = 0.038$  are introduced into the function  $L_{o5}(k, T_0, T_f, F_p, F_v)$ . The relationship between  $h_b$ ,  $T_v$ , and  $F_v$  can be obtained.

Fig. 8 shows the relationship among  $L_{o5}$ ,  $T_v$ , and  $F_v$  for different slopes ( $\theta_s = 0^\circ, 5^\circ, 10^\circ, 15^\circ, 20^\circ, 25^\circ$ , and  $30^\circ$ ). It can be seen that the vane does not extend when  $T_v$  and  $F_v$  are small. When  $T_v$  and  $F_v$  reach a certain value, the vane starts to extend, and the vane extends more with an increase of  $T_v$  and  $F_v$  [52,53]. In Fig. 8, different colors represent different slopes; they do not coincide. This situation is mainly caused by the change in the contact point between the wheel and slope [54].

Fig. 9 shows the relationship between the extension length  $L_{o5}$  and the inserting depth  $h_b$ . There are 21 values of the inserting depth  $h_b$ . It can be seen that each value does not exceed its corresponding surface, which means that  $h_b \leq L_{o5}$ . This indicates that

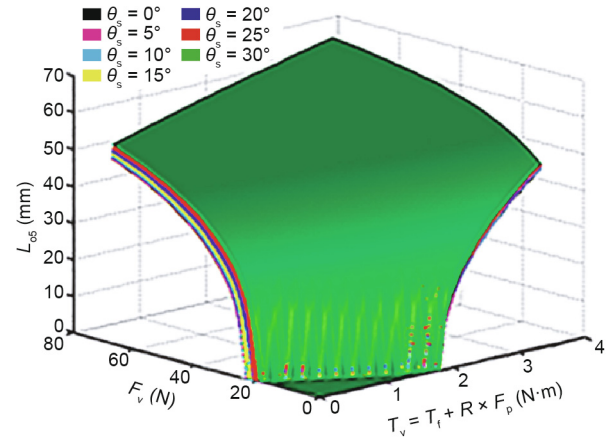


Fig. 8. Relationship among  $L_{o5}$ ,  $T_v$ , and  $F_v$  for different slopes of the front wheel.

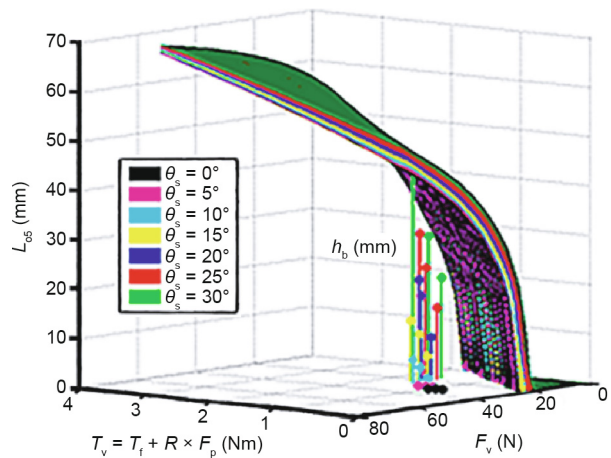


Fig. 9. Relationship between the extension length  $L_{o5}$  and the inserting depth  $h_b$ .

the vane-telescopic walking wheel can smoothly pass through the 21 kinds of road conditions [55,56]. In addition, it is clear that the maximum among the 21 values is in contact with its corresponding surface, which indicates that the wheel's energy consumption has been reduced to the lowest level.

Using the same optimization method, the spring stiffness  $k$  and initial torque value  $T_0$  of the middle wheel are  $k = 0.135 \text{ N}\cdot\text{m}\cdot\text{rad}^{-1}$  and  $T_0 = -0.023 \text{ N}\cdot\text{m}$ , and those of the rear wheel are  $k = 0.218 \text{ N}\cdot\text{m}\cdot\text{rad}^{-1}$  and  $T_0 = -0.128 \text{ N}\cdot\text{m}$ .

4.3. Experiments with the vane-telescopic walking wheel

To test the actual performance and reliability of the vane-telescopic walking wheel, a prototype of the vane-telescopic walking wheel with the same dimensions was manufactured and installed on the lunar rover prototype CJ-1 (Fig. 10). An experiment on simulated lunar soil was carried out at the lunar surface simulation test field at the China Institute of Space Technology (Fig. 11).

During the test, when the lunar rover normally runs in the soil, the length of the wheel vane increases to maintain proper thrust, as shown in Fig. 12(a). Then a horizontal force of 300 N is used to pull the wheel to simulate the resistance case. The vane continues to extend and the wheel traction is increased. The increased traction force overcomes the horizontal force so that the prototype can maintain the original speed, as shown in Fig. 12(b). When the horizontal force is gradually reduced, the vane

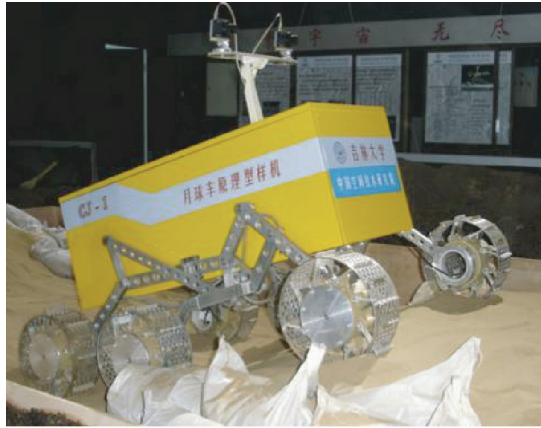


Fig. 10. Prototype of CJ-1.

is gradually restored to its original position, and the energy consumption is reduced, as shown in Fig. 12(c).

The experimental results show that the optimized vane-telescopic walking wheel can control the extension length of the vane according to the terrain resistance. Moreover, the energy consumption of the lunar rover can be effectively controlled when it passes through a complex road.

## 5. Conclusions

In this paper, an effective vane-telescopic walking wheel is proposed. This new walking system design method can provide a useful reference for solving the issues of trafficability and climbing ability for a lunar rover in complex terrain on the moon, while minimizing energy consumption. This was achieved through numerical simulation and system testing. First, we set up an experimental prototype, named CJ-1, to analyze the existing mechanical design. Based on the CJ-1 lunar rover prototype, a new vane-telescopic walking wheel was proposed with a positive and negative

quadrangle suspension, especially designed for the complex terrain on the moon. Second, we analyzed the wheels' force for the lunar rover. Furthermore, the parameter optimization of the vane-telescopic walking wheel was analyzed and simulated. Finally, a realistic moon environment was set up to demonstrate the effectiveness of the proposed wheel system.

In future work, we aim to establish a more realistic and comprehensive test ground to simulate the lunar surface environment. More types of lunar soil can be added to allow the experiment to comprehensively simulate the real driving situation of wheels on the lunar surface. Another possible extension is to increase the bearing capacity of the vane-telescopic walking wheel for future manned lunar rovers. The Chang'e project is an important part of the National Key Project, and provides a reference for the new lunar rover design [57–61]. We would also like to have an academic exchange with researchers from all over the world.

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## Compliance with ethics guidelines

Lu Yang, Bowen Cai, Ronghui Zhang, Kening Li, Zixian Zhang, Jiehao Lei, Baichao Chen, and Rongben Wang declare that they have no conflict of interest or financial conflicts to disclose.



Fig. 11. Simulation on a lunar surface.

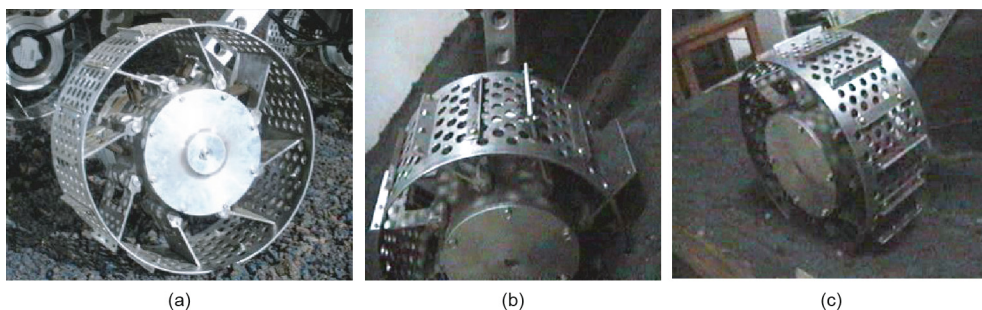


Fig. 12. The vane extension. (a) The length of the vane increases when running in the soil; (b) the vane continues to extend when a horizontal force is used to pull the wheel; (c) the vane is restored when the horizontal force is reduced.

## Nomenclature

$A$	contact area between wheel rim and soil
$b$	vane thickness
$b_1$	width of the wheel rim
$b_2$	vane width
$c$	cohesion force
$D$	diameter of the wheel rim
$F_p$	wheel friction
$F_v$	supporting force
$F_d$	maximum traction force
$F_{Rb}$	bulldozing resistance
$F_{Rc}$	compaction resistance
$F_{Rs}$	slope resistance
$F_{Rv}$	vane resistance
$F_w$	maximum soil thrust on wheel rim
$F_s$	maximum soil thrust on vane
$G$	gravity on one side of the load platform
$h$	eccentricity between the inner wheel and the outer ring
$h_b$	inserting depth of the vane
$k$	vane spring stiffness
$k_c$	cohesion modulus of the soil
$k_\phi$	friction modulus of the soil
$L_o$	length of vane extension
$L_v$	vane length
$L_d$	vane length between the outer ring and the inner wheel
$N$	number of vanes
$n$	soil deformation index
$N_\phi$	flow value
$N_c, N_\gamma$	terzaghi bearing coefficient
$P$	wheel pressure
$q$	pressure stress
$R$	outer ring radius
$r$	inner wheel radius
$S$	slip ratio of the wheel
$T_0$	spring initial torque
$T_f$	wheel rolling resistance torque
$T_v$	rolling friction force
$W_1, W_2, W_3$	weight of front, middle, and rear wheels
$z_0$	sinking depth of the wheel rim
$\gamma_s$	bulk density
$\theta_s$	slope angle
$\phi$	internal friction angle

## Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.eng.2020.07.009>.

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