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# Transparent Thermally Tunable Microwave Absorber Prototype Based on Patterned VO<sub>2</sub> Film



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## ABSTRACT

Transparent microwave absorbers that exhibit high optical transmittance and microwave absorption capability are ideal, although having a fixed absorption performance limits their applicability. Here, a simple, transparent, and thermally tunable microwave absorber is proposed, based on a patterned vanadium dioxide (VO<sub>2</sub>) film. Numerical calculations and experiments demonstrate that the proposed VO<sub>2</sub> absorber has a high optical transmittance of 84.9% at 620 nm; its reflection loss at 15.06 GHz can be thermally tuned from −4.257 to −60.179 dB, and near-unity absorption is achieved at 523.750 K. Adjusting only the patterned VO<sub>2</sub> film duty cycle can change the temperature of near-unity absorption. Our VO<sub>2</sub> absorber has a simple composition, a high optical transmittance, a thermally tunable microwave absorption performance, a large modulation depth, and an adjustable temperature tuning range, making it promising for application in tunable sensors, thermal emitters, modulators, thermal imaging, bolometers, and photovoltaic devices.

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## 1. Introduction

The recent, rapid development of optoelectronic devices, including communication and medical devices, and detectors, has made human life more convenient [1–11]. However, optoelectronic devices emit large amounts of electromagnetic radiation [12–14], leading to electromagnetic interference (EMI). Microwave absorbers that can attenuate and even eliminate the adverse effects of microwave radiation are critical for achieving EMI shielding. It is important for microwave absorbers to exhibit efficient microwave absorption and optical transmittance in many applications involving transparent structures, such as windows for communication, medical, and aerospace equipment [15–18].

Recently, efforts have been made to fabricate optically transparent microwave absorbers [19–22]. Wang et al. [19] proposed a transparent perfect microwave absorber employing an asymmetric resonance cavity using graphene and transparent ultrathin doped silver, achieving 99.50% absorption at 13.75 GHz and 93.50%

relative visible transmittance. Lai et al. [20] developed an optical transparent flexible broadband absorber based on the indium tin oxide (ITO)–polyethylene terephthalate–ITO structure that achieves a wide absorption bandwidth from 19.9 to 51.8 GHz (absorption > 0.8). However, the transparent microwave absorbers examined rely on geometrical parameters, and thus, once they are designed and fabricated, they exhibit fixed performance characteristics with a constant operating frequency or absorptivity.

Various microwave absorbers with tunable frequency and absorptivity have been recently proposed, with research following two main approaches. In the first approach, various lumped tuning elements, such as varactors and positive–intrinsic–negative (PIN) diodes, are adopted in the structure [23–29]; in this case, tunable microwave absorber performance is achieved by changing the bias voltages applied to the lumped elements. However, this type of absorber requires a complex feed network that is difficult to fabricate and a biasing circuit; generally, such a structure is nontransparent because of the opaque lumped elements. The second approach uses active-controlled materials, such as graphene [29–37], ferroelectric materials [38,39], liquid crystals [40,41], and phase-change materials [42–57]. Among these, VO<sub>2</sub> is a promising candidate for tunable absorbers owing to its drastic

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insulator-to-metal phase transition (at  $\sim 340$  K) that leads to transitioning of the sheet resistance magnitude (theoretically five orders of magnitude) and various transition-triggering mechanisms (such as thermal heating, optical excitation, and bias voltage). However, most studies on VO<sub>2</sub> tunable absorbers have focused on the terahertz [42–48] and infrared bands [49–57]; particularly, the experimental verification of VO<sub>2</sub> tunable absorbers requires further reporting. In the few reported experiments on VO<sub>2</sub> tunable terahertz absorbers, the absorbers utilize complete VO<sub>2</sub> films, resulting in an opaque tunable terahertz absorber since the VO<sub>2</sub> film optical transmission is almost zero in the visible band. To the best of our knowledge, the use of VO<sub>2</sub> tunable microwave absorbers for visual observation remains unreported.

Here, a transparent thermally tunable microwave absorber is proposed for the first time based on a patterned VO<sub>2</sub> film that has a simple structure comprising a top-patterned VO<sub>2</sub> film, transparent substrate (quartz glass), and bottom transparent reflective layer (double-layer ITO (D-ITO)). Thermally controlling the VO<sub>2</sub> film sheet resistance enabled the microwave reflection loss (RL) amplitude to be tuned from  $-4.257$  to  $-60.179$  dB. Particularly, a near-unity (99.993%) absorption peak at 15.060 GHz was achieved at 523.750 K, while the optical transmittance was 84.900% at 620.000 nm. Furthermore, the temperature required to achieve near-unity absorption can be tuned by varying the patterned VO<sub>2</sub> film duty cycle. The superior characteristics of the proposed VO<sub>2</sub> absorber suggest that it can be promising for transparent tunable microwave absorbers.

## 2. Methods

### 2.1. Fabricating VO<sub>2</sub> films

We deposited the VO<sub>2</sub> films on quartz glass (silicon dioxide, 15.6 mm  $\times$  7.7 mm) using a high-power impulse magnetron sputtering system (MS650C; Shengyang KEYOU Vacuum Technology Co., Ltd., China) with a pure vanadium target (99.99%, 3.00 in (1 in = 2.54 cm); Beijing Gold Crown for the New Material Technology Co., Ltd., China). The sputtering deposition temperature and duration were 823.15 K and 55.00 min, respectively. We fixed the power, pulse width, and frequency at 200 W, 50  $\mu$ s, and 200 Hz, respectively. The working pressure was set to 0.9 Pa using pure argon (Ar) and oxygen (O<sub>2</sub>) at a ratio of 80.0/0.4.

### 2.2. Fabricating VO<sub>2</sub> absorber sample

The fabrication process for the VO<sub>2</sub> absorber sample can be divided into two stages: fabricating the transparent reflective layer at the bottom and the patterned VO<sub>2</sub> films on the top. The transparent reflective layer that acts as a heater is composed of ITO (8  $\Omega$  per square ( $\Omega$ -sq<sup>-1</sup>), 40 mm  $\times$  40 mm; Luoyang Shangzhuo Technology Co., Ltd., China) and aluminum foil (20 mm  $\times$  20 mm; Shenzhen Jingzhe Technology Co., Ltd., China). The aluminum foil was cut into a long strip of 0.8 mm  $\times$  10.0 mm and pasted onto the ITO film surface using conductive silver paint (Ag and Cu; Jinyi Technology Co., Inc., China), as shown in Fig. S1 in Appendix A. The aluminum foil and ITO were fixed for 15 h at 30 °C to ensure a reliable electrical connection between them.

Patterned VO<sub>2</sub> samples with different duty cycles were fabricated using the same process. First, we pretreated the VO<sub>2</sub> film surface, and a photoresist layer (1  $\mu$ m thick, AR4400-05 photoresist) was patterned using vacuum contact lithography (URE-2000/35 L; Institute of Optics and Electronics, Chinese Academy of Sciences, China) and the corresponding chromium masks. Then, the VO<sub>2</sub> film without photoresist protection was etched using a reactive ion etching machine (ME-3A; Institute of Microelectronics, Chinese

Academy of Sciences, China). The working pressure, power, and duration of etching were 5 mTorr (1 mTorr = 0.133 Pa), 100 W, and 1 min, respectively. Pure sulfur hexafluoride (SF<sub>6</sub>) and O<sub>2</sub> were used as the etching gases at flow rates of 54 and 6 standard cubic centimeters per minute (sccm), respectively. Patterned VO<sub>2</sub> samples were obtained after removing the photoresist.

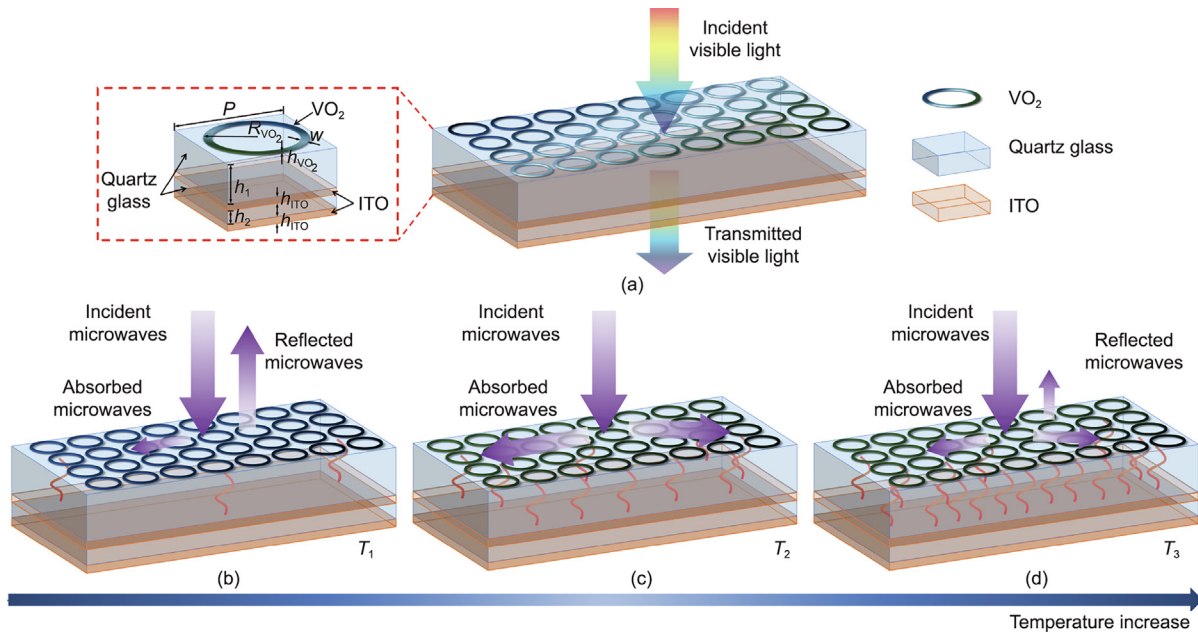
### 2.3. Sample characterization

The optical transmittance of the VO<sub>2</sub> absorber sample was measured using an ultraviolet (UV)–visible (VIS)–near-infrared (NIR) spectrophotometer (Lambda 950 UV/VIS/NIR Spectrometer, PerkinElmer, USA). The VO<sub>2</sub> absorber was microwave characterized (RL and shielding effectiveness (SE)) in the Ku band utilizing a vector network analyzer (E5071C; Keysight, USA; 300 kHz–20 GHz) with a Ku band-slotted waveguide (HD-140WCAN, Henda Microwave, China). We used a double-testing digital four probe tester (ST2263, Suzhou Jingge Electronic Co., Ltd., China) to measure the square resistance of the VO<sub>2</sub> film at various temperatures. The VO<sub>2</sub> content in the film was determined by X-ray photoelectron spectroscopy (XPS; EscaLab 250Xi; Thermo Fisher Scientific, USA). The XPS data were calibrated to the C1s peak and analyzed using the XPSPEAK software. The fabricated VO<sub>2</sub> absorber sample was micrographed using a three-dimensional (3D) measuring laser microscope OLS5000 (Olympus Corporation, Japan). The Raman spectra of the VO<sub>2</sub> films and patterned VO<sub>2</sub> film were measured using a micro-Raman spectrometer (Renishaw inVia Reflex; Renishaw, UK) with 532 nm laser wavelength.

## 3. Absorber design and theoretical analysis

### 3.1. Absorber design

A schematic diagram of the proposed transparent thermally tunable microwave absorber based on a patterned VO<sub>2</sub> film is shown in Fig. 1. The absorber consists of three layers: The top, middle, and bottom layers are a patterned VO<sub>2</sub> film, transparent substrate, and transparent reflective layer, respectively. In this study, thermal heating is the transition-triggering mechanism for the insulator-to-metal phase transition of the VO<sub>2</sub> film, and the independent small rings in Fig. 1 represent the patterned VO<sub>2</sub> film that shows color changes from dark gray (Fig. 1(b)) to dark green (Figs. 1(c) and (d)) with increasing temperature (Fig. S2 in Appendix A). The patterned VO<sub>2</sub> film comprises an array of unit cells. The unit cell of the proposed tunable absorber is shown by the red frame in Fig. 1(a). The absorber parameters are as follows: period  $P = 2.000$  mm, ring radius  $R_{VO_2} = 0.995$  mm, VO<sub>2</sub> film thickness  $h_{VO_2} = 200.000$  nm, quartz glass thickness between the VO<sub>2</sub> film and ITO  $h_1 = 2.500$  mm, thickness of the ITO film  $h_{ITO} = 200.000$  nm, and quartz glass thickness between the two layers of the D-ITO  $h_2 = 1.400$  mm. The VO<sub>2</sub> film used here is a monoclinic phase VO<sub>2</sub> film that displays phase transition behavior (the Raman spectra of the VO<sub>2</sub> film at different temperatures and the Raman spectra of the patterned VO<sub>2</sub> film are shown in Figs. S3 and S4 in Appendix A). The measured sheet resistance of the VO<sub>2</sub> film shows a transition of three orders of magnitude caused by heating and cooling, resulting in a value less than that achieved by the theoretical resistance transition of five orders of magnitude, as shown in Fig. 2(a). This is because the VO<sub>2</sub> content of the film used is only 73.2% (the content was calculated based on the ratio of the areas under the VO<sub>2</sub> peaks to the total area under all of the peaks, as shown in Fig. S5 in Appendix A). The D-ITO, which has a high normalized optical transmittance of 94.29% at 620.00 nm (Fig. S6 in Appendix A) and an electromagnetic SE of more than 40 dB (Fig. S7 in Appendix A) in the Ku band (12–18 GHz), was selected as the transparent reflective layer. Quartz glass was the transparent substrate adopted to separate the



**Fig. 1.** Transparent thermally tunable microwave absorber based on a patterned VO<sub>2</sub> film. (a) Schematic diagram of the absorber. The red frame shows the unit cell of the absorber. (b–d) Schematic diagram of the absorber under three typical temperatures ( $T_1$ ,  $T_2$ , and  $T_3$ ),  $T_1 < T_2 < T_3$ ; as the temperature increases, the absorber exhibits different microwave absorption performances with different absorption amplitudes. (b) At  $T_1$ , which is close to 302.15 K, most of the incident microwave is reflected. (c) At a given temperature  $T_2$ , the incident microwave is almost completely absorbed. (d) At  $T_3 > T_2$ , most of the incident microwave is absorbed, and the rest is reflected.  $P$ : period;  $h_1$ : quartz glass thickness between the VO<sub>2</sub> film and ITO;  $h_2$ : quartz glass thickness between the two layers of the D-ITO;  $h_{ITO}$ : thickness of the ITO film;  $R_{VO_2}$ : ring radius;  $h_{VO_2}$ : VO<sub>2</sub> film thickness;  $w$ : ring linewidth.

patterned VO<sub>2</sub> film from the transparent reflective layer. Moreover, D-ITO acted as a heater, as shown in Fig. S1, and aluminum foil was used as the electrode to supply voltage to D-ITO to achieve different temperatures.

### 3.2. Theoretical analysis

The transfer matrix method is a powerful tool to analyze the absorption performance of microwave absorbers. A transfer matrix method based on the equivalent circuit and transmission line theories was adopted to extract the sheet resistance and frequency-dependent absorption of the VO<sub>2</sub> absorber. As shown in the red frame in Fig. 2(b), the patterned VO<sub>2</sub> film on the top layer was modeled as a series equivalent circuit composed of inductance  $L_1$ , capacitance  $C_1$ , and resistance  $R_1$  based on the equivalent circuit theory [58]. The values of  $L_1$  and  $C_1$  are influenced by the shape and dimensions of the patterned VO<sub>2</sub> film, whereas the value of  $R_1$  depends on the duty cycle  $D$  and sheet resistance  $R_S$  of the VO<sub>2</sub> film, and  $R_1 = R_S/D$ . The equivalent impedance  $Z_1$  of the patterned VO<sub>2</sub> can be expressed as [58]

$$Z_1 = R_1 + j\omega L_1 + \frac{1}{j\omega C_1} \quad (1)$$

where  $j$  is an imaginary unit.  $\omega = 2\pi f$  is the angular frequency of the incident wave.  $f$  is the microwave frequency.

According to the transmission line theory, the transfer matrix  $[V]$  of the patterned VO<sub>2</sub> film is given by

$$[V] = \begin{pmatrix} 1 & 0 \\ \frac{1}{Z_1} & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ \frac{1}{R_1 + j\omega L_1 + \frac{1}{j\omega C_1}} & 1 \end{pmatrix} \quad (2)$$

Both quartz glass and the ITO film can be regarded as transmission lines with certain lengths and characteristic impedances, and their transfer matrix is expressed as [59]

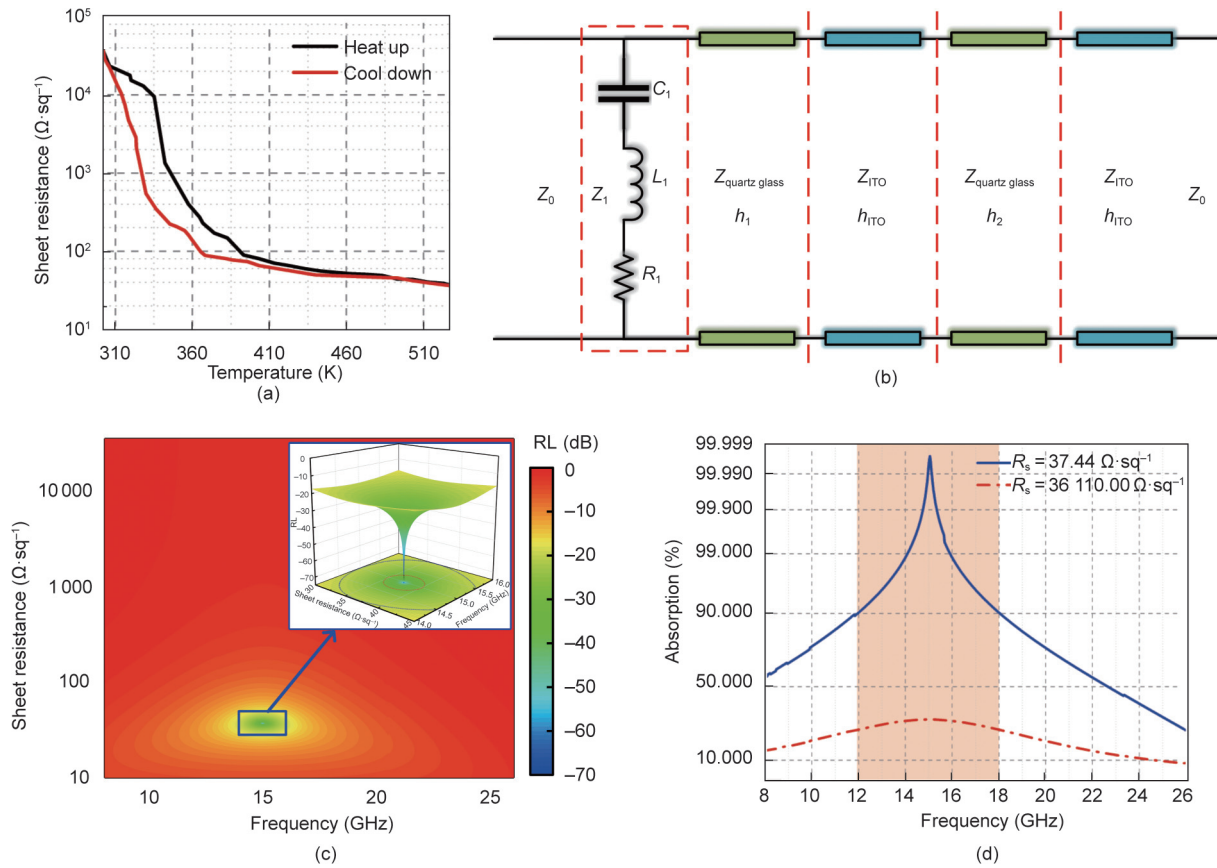
$$\begin{pmatrix} \cosh \gamma h & -Z \sinh \gamma h \\ -\frac{1}{Z} \sinh \gamma h & \cosh \gamma h \end{pmatrix}^{-1} \quad (3)$$

where  $Z$  is the normalized characteristic impedance,  $\gamma$  is the propagation constant of the material, and  $h$  is the thickness of the material.  $Z$  and  $\gamma$  are expressed as

$$\begin{aligned} Z &= \frac{1}{Z_0} \sqrt{\frac{\mu}{\epsilon}} = \frac{1}{Z_0} \sqrt{\frac{\mu}{\epsilon' + j\sigma/\omega}} \\ \gamma &= \omega \sqrt{\mu \epsilon} = \omega \sqrt{\mu(\epsilon' + j\sigma/\omega)} \\ \sigma &= \frac{1}{\rho} = \frac{1}{R_S h} \end{aligned} \quad (4)$$

where  $Z_0 = 377 \Omega$  is the impedance of free space,  $\epsilon$  is the permittivity,  $\epsilon'$  is the real part of the permittivity,  $\mu$  is the permeability of free space,  $\sigma$  is the electric conductivity, and  $\rho$  is the resistivity. The electric conductivity  $\sigma$  is inversely related to the resistivity  $\rho$  and sheet resistance  $R_S$  (see Note. S1 in Appendix A for simplification). Based on Eqs. (1)–(4), the total transfer matrix  $[M]$  of the patterned VO<sub>2</sub> absorber is related to the transfer matrices of each section as follows:

$$\begin{aligned} [M] &= \begin{pmatrix} 1 & 0 \\ \frac{1}{R_1 + j\omega L_1 + \frac{1}{j\omega C_1}} & 1 \end{pmatrix} \\ &\times \begin{pmatrix} \cosh \gamma_{\text{quartz}} h_1 & -Z_{\text{quartz glass}} \sinh \gamma_{\text{quartz}} h_1 \\ -\frac{1}{Z_{\text{quartz glass}}} \sinh \gamma_{\text{quartz}} h_1 & \cosh \gamma_{\text{quartz}} h_1 \end{pmatrix}^{-1} \\ &\cdots \times \begin{pmatrix} \cosh \gamma_{ITO} h_{ITO} & -Z_{ITO} \sinh \gamma_{ITO} h_{ITO} \\ -\frac{1}{Z_{ITO}} \sinh \gamma_{ITO} h_{ITO} & \cosh \gamma_{ITO} h_{ITO} \end{pmatrix}^{-1} \\ &\times \begin{pmatrix} \cosh \gamma_{\text{quartz}} h_2 & -Z_{\text{quartz glass}} \sinh \gamma_{\text{quartz}} h_2 \\ -\frac{1}{Z_{\text{quartz glass}}} \sinh \gamma_{\text{quartz}} h_2 & \cosh \gamma_{\text{quartz}} h_2 \end{pmatrix}^{-1} \\ &\cdots \times \begin{pmatrix} \cosh \gamma_{ITO} h_{ITO} & -Z_{ITO} \sinh \gamma_{ITO} h_{ITO} \\ -\frac{1}{Z_{ITO}} \sinh \gamma_{ITO} h_{ITO} & \cosh \gamma_{ITO} h_{ITO} \end{pmatrix}^{-1} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \end{aligned} \quad (5)$$



**Fig. 2.** Measured sheet resistance of the VO<sub>2</sub> film, equivalent circuit model, and calculation results of the VO<sub>2</sub> absorber. (a) Measured sheet resistance of the VO<sub>2</sub> film versus temperature. (b) Equivalent circuit model of the VO<sub>2</sub> absorber. (c) Relationship between the sheet resistance of the VO<sub>2</sub> absorber and the calculated absorption results of the VO<sub>2</sub> absorber in the 8–26 GHz band. The inset in (c) is the enlarged 3D view of the contour plots at varying sheet resistances in the range of 30–45 Ω·sq<sup>-1</sup> in the 14–16 GHz band. The contour lines of -20 and -30 dB are plotted by blue and red dashed lines, respectively. (d) Calculated absorption of the VO<sub>2</sub> absorber versus frequency for the sheet resistance values of the VO<sub>2</sub> film of 37.44 and 36 110.00 Ω·sq<sup>-1</sup>. Z<sub>0</sub> = 377 Ω is the impedance of free space; L<sub>1</sub> is the inductance; R<sub>1</sub> is the resistance; C<sub>1</sub> is the capacitance; Z<sub>1</sub> is the equivalent impedance of the patterned VO<sub>2</sub>; Z<sub>quartz glass</sub> is the normalized characteristic impedance of the quartz glass; Z<sub>ITO</sub> is the normalized characteristic impedance of the ITO.

where  $m_{11}$ ,  $m_{12}$ ,  $m_{21}$ , and  $m_{22}$  are the value of the elements of  $[M]$ ,  $\gamma_{\text{quartz}}$  is the propagation constant of the quartz glass,  $Z_{\text{quartz glass}}$  is the normalized characteristic impedance of the quartz glass,  $\gamma_{\text{ITO}}$  is the propagation constant of the ITO,  $Z_{\text{ITO}}$  is the normalized characteristic impedance of the ITO.

According to the relationship between the transfer matrix and the S-parameter matrix, reflection coefficient  $S_{11}$  and transmission coefficient  $S_{21}$  of the absorber can be expressed as follows:

$$S_{11} = \frac{m_{11} + m_{12} - m_{21} - m_{22}}{m_{11} + m_{12} + m_{21} + m_{22}} \quad (6)$$

$$S_{21} = \frac{2}{m_{11} + m_{12} + m_{21} + m_{22}}$$

The RL, SE, and absorptance ( $A$ ) are obtained using the reflection coefficient and transmission coefficient as follows:

$$SE = 10 \times \lg(|S_{21}|^2)$$

$$RL = 10 \times \lg(|S_{11}|^2) \quad (7)$$

$$A = 1 - |S_{11}|^2 - |S_{21}|^2$$

Using the above equations, we calculated the RL at 8–26 GHz versus the sheet resistance. The calculation results show that the RL undergoes a shift as the sheet resistance increases, as shown in Figs. 2(c) and (d). At 302.15 K, the VO<sub>2</sub> films have a maximum sheet resistance of 36 110 Ω·sq<sup>-1</sup> and are insulating, as shown in Fig. 2(a), the calculated reflection capacity of the VO<sub>2</sub> absorber is the highest, whereas its absorption capacity is the lowest. The peak absorption of 28.4% (red dash-dotted line in Fig. 2(d)) is also due to

the absorption capacity of D-ITO (the conductivity of ITO is  $7.14 \times 10^5 \text{ S}\cdot\text{m}^{-1}$ ), and the peak absorption can be reduced by increasing the conductivity of the ITO film (Fig. S8 in Appendix A). As the sheet resistance of the VO<sub>2</sub> films decreases from 36 110.00 to 37.44 Ω·sq<sup>-1</sup>, the peak RL of the VO<sub>2</sub> absorber decreases from -1.451 to -62.870 dB, indicating that the VO<sub>2</sub> absorber has a large modulation depth for RL. As shown in Fig. 2(d), at 37.44 Ω·sq<sup>-1</sup>, the VO<sub>2</sub> films are resistive, and the absorber achieves near-perfect impedance matching to free space, resulting in the best performance of the VO<sub>2</sub> absorber; it achieves a bandwidth of more than 90% absorptance from 11.88 to 18.11 GHz, and the peak absorption is near-unity at 15.05 GHz. However, due to an impedance mismatch occurring with the decrease in VO<sub>2</sub> film sheet resistance, the peak absorption decreases when the VO<sub>2</sub> film sheet resistance decreases further.

The VO<sub>2</sub> film sheet resistance is temperature dependent and decreases monotonically with increasing temperature, as shown in Fig. 2(a). Therefore, the VO<sub>2</sub> absorber exhibits thermally tunable absorption performance, as shown in Fig. 2(c). Additionally, the calculation results show that the VO<sub>2</sub> absorber has a large modulation depth.

### 3.3. Impedance matching analysis

The absorption mechanism is the synergistic result of impedance matching and microwave attenuation capability. The physical cause of microwave attenuation is the Joule heat loss caused by

conductivity, which dissipates microwave energy into heat energy. An equivalent transmission line model was developed to analyze the impedance matching under different frequencies with different sheet resistances (Fig. S9 in Appendix A). Due to the strong electromagnetic SE, the transparent reflective layer of D-ITO is modeled as a short circuit. The input impedance  $Z_{in}$  of the VO<sub>2</sub> absorber can be expressed as  $\frac{1}{Z_{in}} = \frac{1}{Z_1} + \frac{1}{Z_2}$  (where  $Z_2$  is the equivalent impedance consisting of D-ITO short circuit and quartz glass transmission line see Note. S2 in Appendix A for the solution procedure). The reflection coefficient  $r$  is related to the input impedance  $Z_{in}$  and free space impedance  $Z_0$  and can be expressed as  $r = \frac{Z_{in} - Z_0}{Z_{in} + Z_0}$  for the VO<sub>2</sub> absorber. The reflection coefficient  $r$  should be equal to zero to achieve high absorption performance, that is, the real and imaginary parts of impedance matching ( $Z_{in}/Z_0$ ) are close to one and zero, respectively. Fig. 2(c) shows that the absorption is low when the sheet resistance exceeds  $200 \Omega \cdot \text{sq}^{-1}$ , so that the real and imaginary parts of  $Z_{in}/Z_0$  are only analyzed for the sheet resistance in the  $10\text{--}200 \Omega \cdot \text{sq}^{-1}$  range as shown in Figs. 3(a) and (b).

Fig. 3 demonstrates that the VO<sub>2</sub> absorber achieves perfect impedance matching at 15.05 GHz with a real part of 1 and an imaginary part of 0 when the sheet resistance is  $34.20 \Omega \cdot \text{sq}^{-1}$ . The sheet resistance is lower than the value  $37.44 \Omega \cdot \text{sq}^{-1}$  obtained by the transfer matrix method; this is because the transmission line method models D-ITO as a short circuit, idealizing the conductivity of D-ITO.

## 4. Results

### 4.1. Experimental verification

To experimentally demonstrate the high optical transmittance and thermally tunable absorption performance of the proposed VO<sub>2</sub> absorber, we fabricated a VO<sub>2</sub> absorber sample and measured its optoelectronic properties. The inset of Fig. 4 (a) shows that the fabricated VO<sub>2</sub> absorber sample exhibits good optical transparency, such that the logo below the sample can be seen with the naked eye. Figs. S10–S12 in Appendix A show the photographs and micrographs of the fabricated VO<sub>2</sub> absorber sample. Fig. 4 (a) shows the transmittance spectra of the fabricated VO<sub>2</sub> absorber sample in the range of 300.00–1000.00 nm at 303.15 and 390.00 K (higher than the phase transition temperature). At 303.15 K, the average normalized transmittance is approximately 77% in the visible range (380–780 nm), the normalized transmittance reaches 78.89% at 550.00 nm (the most sensitive wavelength to the human eye), and the peak normalized transmittance reaches 84.9% at 620.0 nm. The fluctuation in the optical transmittance is due to the optical performance of D-ITO (Fig. S6). The transmittance spectrum at 390.00 K is almost coincident with that at 303.15 K,

indicating that the temperature negligibly influences the visible transmittance.

The microwave absorption performance of the fabricated VO<sub>2</sub> absorber samples was measured using a vector network analyzer system. Figs. 4(b) and (c) and Fig. S13 in Appendix A show the contour plots of the measured RL and SE versus frequency and temperature, respectively. The SE is less than  $-40$  dB for all measurements in the temperature range of 303.15–524.85 K, indicating almost zero transmission. The absorption is approximately estimated by  $A = 1 - R$ , where  $R$  is the reflectivity and calculated as  $R = 10^{\frac{RL}{10}} \times 100\%$  using the measured RL. Near 303.15 K, the VO<sub>2</sub> film exists in insulator phase and the peak RL of the fabricated VO<sub>2</sub> absorber sample is  $-4.257$  dB. Moreover, the RL of the fabricated VO<sub>2</sub> absorber sample agrees with that of the D-ITO absorber (Fig. S14 in Appendix A) composed of quartz glass with the same thickness and D-ITO, demonstrating that, at 303.15 K, the absorption capacity is attributed to D-ITO, and the patterned VO<sub>2</sub> film has little effect. The fabricated VO<sub>2</sub> absorber sample exhibited a variation of approximately  $-55.922$  dB in the peak RL (from  $-4.257$  to  $-60.179$  dB) at 15.06 GHz when the temperature increased from 303.15 to 523.75 K, indicating that the VO<sub>2</sub> absorber exhibits thermally tunable absorption and a large modulation depth. The fabricated VO<sub>2</sub> absorber sample achieved a SE and RL of  $-41.756$  and  $-60.179$  dB, respectively, and an absorption of 99.993% at 15.060 GHz when the temperature was 523.750 K. At this temperature, VO<sub>2</sub> exists in the metallic phase, allowing the absorber to perfectly match the free space to achieve peak absorption. The absorption bandwidth of the fabricated VO<sub>2</sub> absorber sample reaches approximately 5.22 GHz (corresponding to the range of 12.72–17.94 GHz, as shown in Fig. 4(d) for absorption  $\geq 90\%$ , almost covering the full Ku band). The peak absorption decreased to 99.990% when the temperature was increased above 524.850 K, possibly due to impedance mismatch. The measured results agree with the calculated predictions shown in Fig. 2(d) and validate the thermally tunable absorption performance and large modulation depth of the proposed absorber. Besides, according to the temperature-dependent reproducibility experiments of the fabricated VO<sub>2</sub> absorber sample (Fig. S15 in Appendix A), the proposed absorber is reusable and stable when temperature cycling, making it is extremely valuable for practical applications.

Additionally, the change in RL with temperature variation is due to the change in impedance matching conditions at the interface between free space and the absorber and the change in impedance matching conditions caused by the different sheet resistances of the VO<sub>2</sub> film. A comparison of Figs. 4(b) and (c) shows that the temperature-dependent RL during the heating process is slightly different from that during the cooling process at the same temperature. This is because the sheet resistance exhibits a small hysteresis, as shown in Fig. 2(a), such that the temperature required to

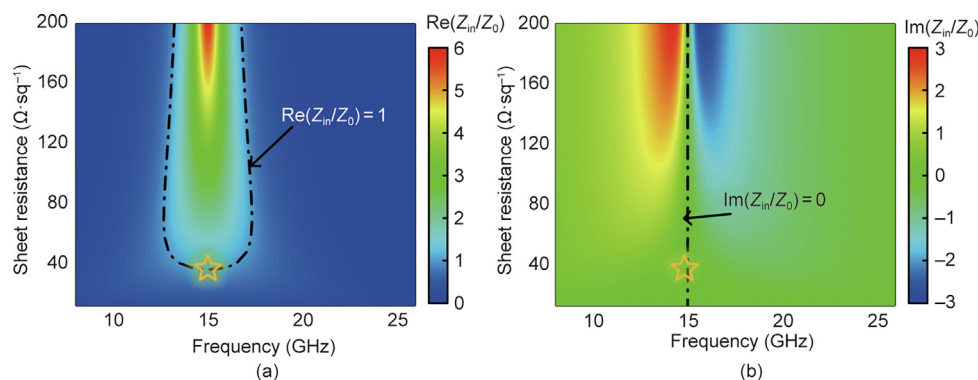
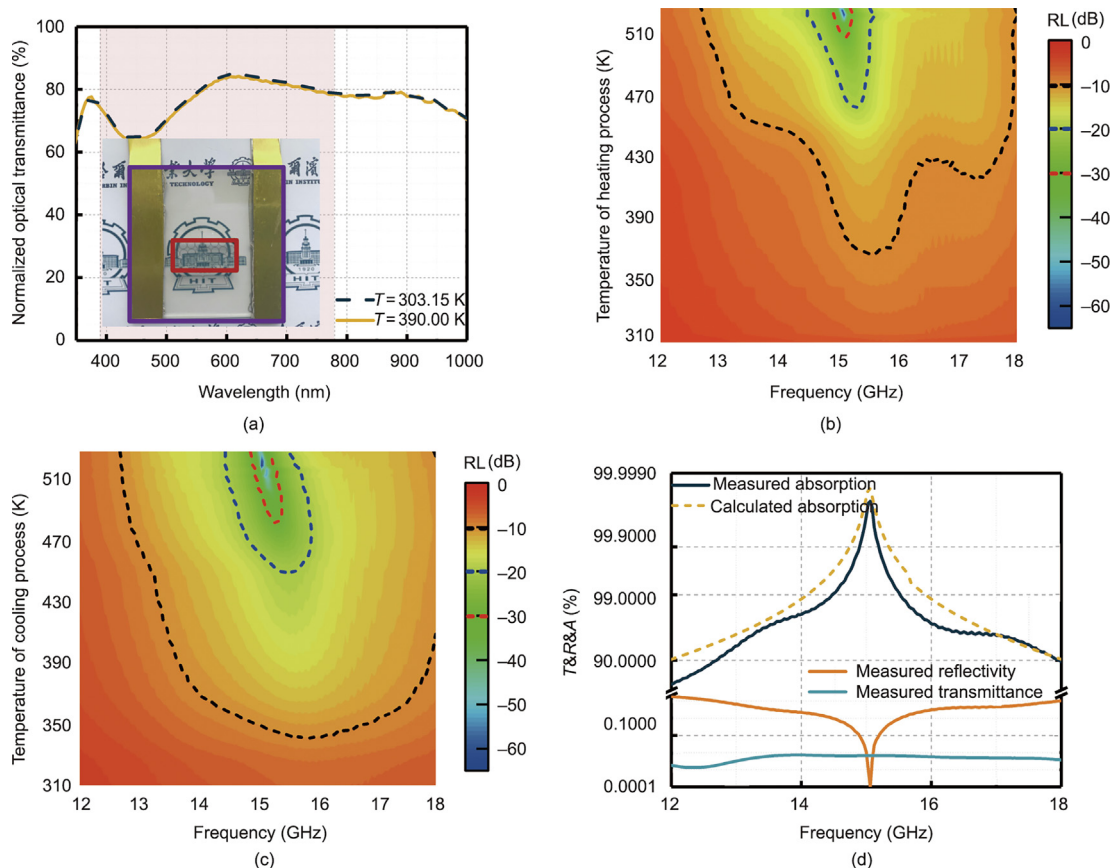


Fig. 3. Relationship between the VO<sub>2</sub> film sheet resistance and the calculated results of impedance matching degree ( $Z_{in}/Z_0$ ) when the VO<sub>2</sub> film sheet resistance is between 10 and  $200 \Omega \cdot \text{sq}^{-1}$ . (a) The real parts; (b) the imaginary parts. Re: real part; Im: imaginary part.



**Fig. 4.** Measured optical transmittance and microwave absorption of the fabricated VO<sub>2</sub> absorber sample. (a) Normalized optical transmittance; the pink shaded area is the area of the visible band, and the inset is a photograph of the VO<sub>2</sub> absorber. The inset in (a) shows a photograph of the fabricated absorber sample (the original photograph in Fig. S10 in Appendix A). The D-ITO sample is framed in purple, and the VO<sub>2</sub> absorber sample is framed in red. Contour plots of the RL versus frequency and temperature of the fabricated VO<sub>2</sub> absorber sample during the (b) heating process and (c) cooling process. The contour lines of -10, -20, and -30 dB are plotted with black, blue, and red dashed lines, respectively. (d) Comparison of the measured absorption, reflectivity, and transmittance at 523.75 K and calculated absorption at a sheet resistance of 37.44 Ω·sq<sup>-1</sup>. T&R&A: transmittance & reflectivity & absorption.

achieve a certain sheet resistance in the heating process is higher than that in the cooling process. Therefore, the RL changes slower during the cooling process.

#### 4.2. Adjustable temperature tuning range

The VO<sub>2</sub> absorber sample fabricated in this study achieved a high optical transmittance, thermally tuned absorption performance, and large modulation depth. However, the temperature tuning range and the temperature to achieve near-unity absorption of this absorber were fixed at 303.15–524.85 and 524.85 K, respectively. The temperature tuning range is determined by the temperature that achieves near-unity absorption. To adapt to different thermal environments and broaden the application of our tunable VO<sub>2</sub> absorber, we investigated a method to achieve an adjustable temperature for near-unity absorption. According to the mechanism of near-unity absorption, achieving a perfect match with free space at different temperatures is vital.

According to Eq. (5), near-unity absorption should be constant if  $R_1$  is maintained.  $R_1$  depends on  $R_1 = R_s/D$ , and  $R_s$  changes with temperature; therefore, adjusting  $D$  with temperature will ensure that  $R_1$  remains constant at different temperatures. We fabricated and measured the microwave absorption performance of three VO<sub>2</sub> absorber samples with  $D$  values of 20%, 50%, and 100% to verify that the near unity absorption temperature can be adjusted using  $D$ . For the patterned VO<sub>2</sub> film shown in Fig. 1(a), to obtain different  $D$  values, we changed only the linewidth of the ring  $w$ . Figs. 5(a)–(f) and Fig. S16 in Appendix A show that all the fabricated VO<sub>2</sub> absorber

samples achieved more than 99.99% peak absorption, thermally tunable absorption performance, and large modulation depth.

To evaluate the relationship between  $D$  and the near-unity absorption temperature, we extracted the temperature-dependent RL of the fabricated VO<sub>2</sub> absorber samples at a near-unity absorption frequency point, as shown in Fig. 5(g). The near-unity absorption temperature increased with decreasing  $D$ , indicating that varying  $D$  adjusts the temperature for the near-unity absorption and tuning range.

Next, we examined the RL of the D-ITO absorber sample (same as the VO<sub>2</sub> absorber, without the patterned VO<sub>2</sub> film) as shown by the purple lines in Fig. 5(g) and Fig. S17 in Appendix A for comparison, to further reveal that the thermally tunable absorption performance of the proposed absorber is attributed to the introduction of the patterned VO<sub>2</sub> film. A slight change in the peak RL for the D-ITO absorber sample was observed at varying temperatures due to the increased temperature that enhanced the electron activity. Additionally, the RL of quartz glass of the same thickness as the Cu foil (brown lines in Fig. 5(g) and Fig. S18 in Appendix A) changed slightly at different temperatures, indicating that quartz glass barely affects the measurements.

### 5. Discussion and conclusions

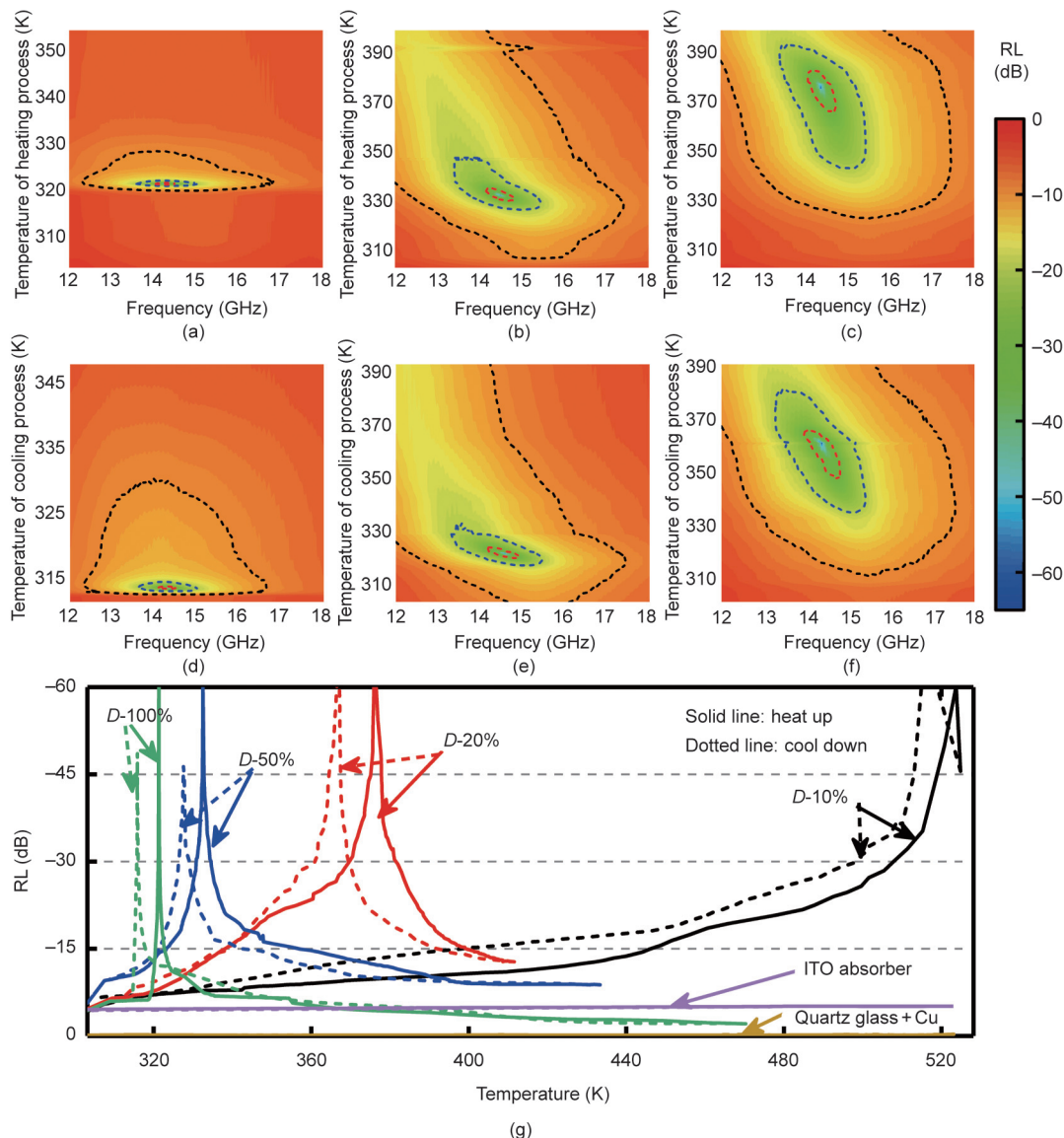
In practice, complex electromagnetic environments have become interested in microwave absorbers. To achieve the optical transmittance required in many application scenarios, an ideal transparent microwave absorber should have a high optical

transmittance. However, transparent microwave absorbers have limited application due to the lack of tunable absorption performance and large modulation depth. Therefore, realizing a microwave absorber with tunable microwave absorption, high optical transmittance, and a large modulation depth is challenging. The main objective of this study was to realize a transparent thermally tunable microwave absorber prototype based on a patterned VO<sub>2</sub> film that simultaneously exhibits a high optical transmittance, a thermally tunable microwave absorption performance, a large modulation depth, and an adjustable temperature tuning range. Numerical calculations and experimental results demonstrate that the proposed VO<sub>2</sub> absorber achieved an 84.900% normalized optical transmittance at 620.000 nm, a near unity (99.993%) absorption peak at 15.060 GHz, and a large modulation depth (55.922 dB) by controlling the temperature from 303.150 to 523.750 K. Furthermore, the temperature for near-unity absorption and its tuning range can be adjusted by varying the VO<sub>2</sub> film duty cycle.

The impedance matching and temperature-dependent sheet resistance of the VO<sub>2</sub> films cause thermally tunable microwave

absorption. Unlike other VO<sub>2</sub> absorbers that are opaque and mainly operate in the terahertz or infrared bands, the VO<sub>2</sub> film in this study was used for the first time in a transparent microwave absorber, and the mechanism of thermally tunable absorption performance was thoroughly analyzed. Additionally, although the patterned VO<sub>2</sub> films play a vital role and form the basis of the proposed absorber prototype, a range of different materials can be used for the transparent substrate and transparent reflective layer to meet the requirements of particular applications. According to the design principle, near-unity absorption can also be extended to other frequencies by controlling the transparent substrate optical thickness, further extending the applicability of this absorber.

In summary, the proposed transparent thermally tunable microwave absorber prototype offers new opportunities for realizing promising transparent, tunable, near-unity microwave absorbers with many potential applications, such as those in temperature sensors, thermal emitters, thermal imaging, and photovoltaic devices.



**Fig. 5.** Temperature and *D*-value dependence of the RL of the fabricated samples. Contour plots of the RL versus frequency and temperature of the fabricated VO<sub>2</sub> absorber sample during the heating process with *D* values of (a) 100%, (b) 50%, and (c) 20%. Contour plots of the RL versus frequency and temperature of the fabricated VO<sub>2</sub> absorber sample during the cooling process with *D* values of (d) 100%, (e) 50%, and (f) 20%. The contour lines of -10, -20, and -30 dB are plotted with black, blue, and red dashed lines, respectively. (g) Temperature-dependent RL of the fabricated VO<sub>2</sub> absorber samples at a near-unity absorption frequency point. *D*: duty cycle of the VO<sub>2</sub> film.

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## Compliance with ethics guidelines

Zhengang Lu, Yilei Zhang, Heyan Wang, Chao Xia, Yunfei Liu, Shuliang Dou, Yao Li, and Jiubin Tan declare that they have no conflict of interest or financial conflicts to disclose.

## Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.eng.2022.10.005>.

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